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**Label:** Article **Jahr:** 1974

**PURL:** https://resolver.sub.uni-goettingen.de/purl?316342866\_0015|log64

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# COMMENTATIONES MATHEMATICAE UNIVERSITATIS CAROLINAE 15,4 (1975)

Each concrete category has a representation by  $\mathbf{T_2}$  paracompact topological spaces

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Abstract: It is shown that every concrete category can be fully embedded into a category whose objects are paracompact Hausdorff spaces and whose morphisms are all nonconstant continuous (or closed continuous) mappings between these spaces.

Key words: Concrete category, full embedding, paracompact Hausdorff space, continuous mapping, closed continuous mapping.

AMS: Primary 54H10, 54G15

Ref. Ž. 3.963.5

3.969

The aim of the paper is to prove that each concrete category is isomorphic to a category whose objects are paracompact connected Hausdorff spaces and whose morphisms are all non-constant continuous (closed continuous, respectively) mappings between these objects. The theorem is based on the fact that each concrete category is fully embeddable into  $S(P_2)$  proved in [3] by Kučera.

A similar result was obtained by V. Trnková [5] who proved an analogical theorem for metric (or compact Hausdorff) spaces under the assumption of the non-existence proper class of measurable cardinals. The present results do not require any special set-theoretical assumption.

The author would like to express his gratitude to V. Trnková who introduced him to this problematics.

<u>Convention</u>: Denote  $P_A = \langle -, A \rangle$  the contravariant hom-functor from the category of all sets and their mappings into itself.

Definition. Let F be a contravariant functor from sets to sets. Denote S(F) the category, objects of which are couples  $(X,\mathcal{U})$ , X being a set,  $\mathcal{U} \subset FX$ , and  $f:(X,\mathcal{U}) \longrightarrow (Y,\mathcal{V})$  is a morphism if  $f:X \longrightarrow Y$  is a mapping with  $Ff(\mathcal{V}) \subset \mathcal{U}$ . In particular, objects of  $S(P_2)$  are couples  $(X,\mathcal{U})$ ,  $\mathcal{U} \subset \exp X$  and morphisms  $f:(X,\mathcal{U}) \longrightarrow (Y,\mathcal{V})$  are mappings such that  $f^{-1}(A) \in \mathcal{U}$  for each  $A \in \mathcal{V}$ .

Theorem 1. Every concrete category can be fully embedded into the category  $S(P_2)$  .

Proof: see [3].

Theorem 2. There exists a metric continuum M such that if Z is a subcontinuum of M,  $f:Z \longrightarrow M$  is a continuous mapping then either f is constant or f(x) = x for all  $x \in Z$ . M has  $x_0$  pairwise disjoint subcontinua.

Proof: see [1].

Convention: For a given topological space T,  $T^X$  denote, the topological product of topological spaces  $T_i$ ,  $i \in X$ , where each  $T_i$  is homeomorphic to T. Let  $T_i$ ,  $i \in I$  be topological spaces, then  $\bigvee_{i \in I} T_i$  denote,

the topological sum of topological spaces  $T_i$ ,  $i \in I$ .

<u>Convention</u>: Denote Z the set of all integers. Choose arbitrary but fixed disjoint subcontinua A, B,  $C_z$ ,  $z \in Z$  of M. Notice that the only continuous mappings between these three spaces are constants and the identities of A, B,  $C_z$ ,  $z \in Z$ .

Theorem 3. There exists a full embedding  $\Phi: S(P_2) \longrightarrow S(P_A)$  .

Proof: see [4].

<u>Definition</u>. A topological space T is stiff if every continuous mapping  $f: T \longrightarrow T$  is either the identity or a constant.

Theorem 4. Let T be a stiff Hausdorff space. Let  $f: T^{0} \longrightarrow T$  be a continuous mapping. Then f is either a projection or a constant.

Proof: see [2].

Corollary 5: Let T be a stiff Hausdorff space. Then  $f: T^{0} \longrightarrow T^{R}$  is a continuous mapping if and only if there exists a partial mapping  $q: R \longrightarrow 0$ , and a point  $\alpha \in T^{R}$ ,  $\alpha = \{\alpha_{i}\}_{i \in R}$ , such that for every  $x \in T^{0}$ ,  $f(x) = \eta_{i} = \{\eta_{i}\}_{i \in R}$  where  $\eta_{i} = x_{0}(i)$  if q(i) is defined,  $\eta_{i} = \alpha_{i}$  otherwise.

In particular,  $f: T \longrightarrow T^{N}$  is a continuous mapping if and only if there exists  $N' \subset N$  and  $\alpha = \{\alpha_{i}\}_{i \in N} \in T^{N}$  such that  $f(x) = \eta_{i} = \{\eta_{i}\}_{i \in N}$  and  $\eta_{i} = x$  if  $i \in N^{r}$ ,  $\eta_{i} = \alpha_{i}$  otherwise.

Corollary 6: The only continuous mappings between  $A^N$  and either B or  $C_{z}$ ,  $z\in Z$  , are constants.

Lemma 7. Let K be a subcontinuum of a Hausderff space Q, let  $a, b \in K$ ,  $a \neq b$  such that  $M = K - \{a, b\}$  is open in Q. Then for each continuous mapping  $f: Z \longrightarrow Q$ , where Z is a continuum, either there exists a component H of  $f^{-1}(K)$  such that  $a, b \in f(H)$  or there exists a continuous mapping  $\tilde{f}: Z \longrightarrow Q$  such that  $\tilde{f} = f$  on  $f^{-1}(Q-M)$  and  $\tilde{f}(f^{-1}(K)) \subset \{a, b\}$ .

Proof: see [5].

Construction 8: In each  $C_z$ ,  $z \in Z$ , choose a pair distinct points  $c_z, d_z$  . Define a topological space  $\mathbb{D} = \bigvee_{\mathbf{z} \in \mathbb{Z}} \, \mathbb{C}_{\mathbf{z}} \, / \! \sim \, \, , \, \, \text{where} \, \, \, \, \mathbf{d}_{\mathbf{z}} \sim \, \mathbf{c}_{\mathbf{z}+1} \quad \text{for every} \, \, \, \mathbf{z} \, \in \, \mathbb{Z} \, \, \, .$ Choose distinct points  $a_1, a_2 \in A$ ,  $\mathcal{Y}_1, \mathcal{Y}_2 \in B$ . For given set X define a topological space  $E_X = A^X \sim (B \times \{0, 1\}) / \approx$ , where {0,4} is a discrete topological space and  $\alpha' = \{\alpha'_{\mathbf{x}}\}_{\mathbf{x} \in \mathbf{X}} \approx \{b_{\mathbf{1}}, 0\}, \{b_{\mathbf{2}}, 0\} \approx \{b_{\mathbf{1}}, 1\}, \{b_{\mathbf{2}}, 1\} \approx \overline{\alpha} = \{\overline{\alpha}_{\mathbf{x}}\}_{\mathbf{x} \in \mathbf{X}},$ where  $a_x' = a_1$ ,  $\overline{a}_x = a_2$  for every  $x \in X$ . For each object  $P = (X, \mathcal{U})$  of  $S(P_A)$  denote by  $P^*$  the space  $E_{\chi} \vee (D \times \mathcal{U})$ , where  $\mathcal{U}$  is the discrete topological space with underlying set  $\,\mathcal{U}\,$  . Let  $\,\widetilde{\mathsf{P}}\,$  be a coarser topological space than  $P^*$ : a set V, open in  $P^*$  is open in  $\widetilde{\beta}$  if and only if for each  $u \in \widetilde{\mathcal{U}} \subset A^{\times}$  either  $u \notin V$ or there exists  $m_0$  with  $\bigcup_{m>n_0} C_m \times \text{fulc } V$  and either  $\{\mathcal{L}_{2},0\}\notin V$  or there exists  $m_{1}$  with  $\bigcup_{n< m_{n}} C_{n} \times \mathcal{U} \subset V$ ; clearly  $\widetilde{\mathbf{F}}$  is a connected paracompact Hausdorff space. Define a contravariant functor  $\psi$  from  $\mathcal{S}(P_A)$  into the

category PAR of connected paracompact Hausdorff spaces:  $\psi P = \widetilde{P} , \ \psi f = (P_A f \vee (1_B \times \{0,1\})) / \approx \vee (1_D \times P_A f / \mathcal{U}) / \sim \ ,$ 

where  $\mathbf{1}_{B}$  and  $\mathbf{1}_{D}$  are the identities of B and D. Clearly,  $\psi \mathbf{f}$  is correctly defined and it is a closed continuous mapping.

Evidently the functor  $\psi$  is faithful.

Lemma 9. Let  $f: T \longrightarrow \widetilde{P}$  be a non-constant continuous mapping.

- a) If T = A then  $f(T) \subset A^X$ ;
- b) if T = B then  $f(T) = B \times \{i\}$ , where  $i \in \{0,4\}$ .
- c) If  $T = C_z$  then  $f(T) \subset D \times \{u\}$  for some  $u \in \mathcal{U}$ . In all above cases, f is an embedding.

Proof: Let K, a, & denote one of the following:

- a)  $K = C_z \times \{u\}$ ,  $\alpha = \langle c_z, u \rangle$ ,  $\mathcal{L} = \langle d_z, u \rangle$  for some  $z \in \mathbb{Z}$ ,  $u \in \mathbb{U}$ .
- b)  $K = B \times \{i\}$ ,  $\alpha = \langle b_1, i \rangle$ ,  $b = \langle b_2, i \rangle$  for some  $i \in \{0, 1\}$ .

Suppose that the former case in Lemma 7 takes place, i.e. that there is a component L of  $f^{-1}(K)$  with  $a, k \in f(L)$ . Then we get easily by Theorem 2 that L is homeomorphic to T and f is a homeomorphism of T ento K. Now, suppose that, for all K, a, k as above, the latter case in Lemma 7 takes place.

1) Suppose that f(T) meets the interior of some K, where K is from a). Then apply Lemma 7 on f,  $K' = C_{z-1} \times \{u\}, \langle c_{z-1}, u \rangle, \langle c_{z-1}, u \rangle \text{ to obtain } f$ 

and again Lemma 7 to  $\widetilde{f}$ ,  $K'' = C_{z+1} \times \{u\}$ ,  $\langle c_{z+1}, u \rangle$ ,  $\langle d_{z+1}, u \rangle$  to obtain  $\widetilde{f}$ . Then  $\widetilde{f}$  coincides with f on  $f^{-1}(K)$  and  $\widetilde{f}(T)$  is a continuum which does not meet the interiors of both K' and K'' but it meets the interior of K. Then, as easily seen from the construction of  $\widetilde{f}$ ,  $\widetilde{f}(T) \subset K$ . By Theorem 2,  $\widetilde{f}$  is an embedding of T onto K and  $f = \widetilde{f}$ .

2) Let the assumption of 1) not hold. Then  $f(T) \subset A^{\chi} \cup U \times \{0, 4\}$  as for any continuum which does not meet the interior of any K from a).

Let us apply Lemma 7 on f,  $B \times \{0\}$ ,  $\langle \mathcal{L}_1, 0 \rangle$ ,  $\langle \mathcal{L}_2, 0 \rangle$  to obtain  $\widetilde{f}$  and again Lemma 7 on  $\widetilde{f}$ ,  $B \times \{1\}$ ,  $\langle \mathcal{L}_1, 1 \rangle$ ,  $\langle \mathcal{L}_2, 1 \rangle$  to obtain  $\widetilde{f}$ .

If  $\tilde{\mathbf{f}}$  is constant then clearly  $\mathbf{f}(T) \subset \mathbb{B} \times \{0\}$  and  $\mathbf{f}$  is an embedding by Theorem 2. Analogously, if  $\tilde{\mathbf{f}}$  is constant then  $\tilde{\mathbf{f}}$  is an embedding of T onto  $\mathbb{B} \times \{1\}$  and so is  $\mathbf{f}$ . Let  $\tilde{\mathbf{f}}$  be non-constant. As  $\tilde{\mathbf{f}}(T) \subset \mathbb{A}^X$ , we may apply Corollaries 5, 6. We obtain that  $\tilde{\mathbf{f}}$  is an embedding of T into  $\mathbb{A}^X$  and so is  $\mathbf{f}$ .

Lemma 10. Let  $f: \widetilde{P} \longrightarrow \widetilde{R}$  be a continuous mapping  $P, R \in S(P_A)$  with  $f/B \times \{0\} = 1_{B \times \{0\}}$ . Then there exists  $Q: R \longrightarrow P$  such that  $\psi Q = f$ .

Proof: Lemma 9 implies either  $f/B \times \{1\} = 1_{B \times \{1\}}$  or  $f(B \times \{1\} = \langle \mathcal{L}_1, 1 \rangle)$ . If  $f(B \times \{1\}) = \langle \mathcal{L}_1, 1 \rangle$  then  $f(\overline{a}) = \langle \mathcal{L}_1, 1 \rangle$  and therefore there exists  $\mathcal{L}: A \longrightarrow \widetilde{R}$  such that  $\langle \mathcal{L}_1, 0 \rangle, \langle \mathcal{L}_2, 0 \rangle \in \mathcal{L}(A)$  but this is impossible. Hence  $f/B \times \{1\} = 1_{B \times \{1\}}$ . Denote  $\Delta_X$  the diagonal of  $A^X$ ,  $\Delta_Y$  the diagonal of  $A^Y$ , where  $P = (X, \mathcal{U})$ ,

$$\begin{split} \mathbf{R} &= (Y, \, \mathcal{V}) \, . \, \, \text{We have } \, \mathbf{f}(\Delta_X) = \Delta_Y \quad \text{and so } \, \mathbf{f}(A^X) \subset A^Y \, . \\ \text{Corollary 5 implies that there exists } \, \mathbf{q} : Y \longrightarrow X \quad \text{such that } \\ \mathbf{f}/A^X &= P_A \, \mathbf{q} \, . \quad \text{As } \, \mathbf{f}(\langle \, \mathcal{b}_1 \,, \, 4 \, \rangle) = \langle \, \mathcal{b}_1 \,, \, 4 \, \rangle \quad \text{and } \, \mathbf{f}(A^X) \subset A^Y \,, \\ \mathbf{f}/D \times \{\, \mathcal{U} \,\} \quad \text{is an embedding from } D \times \{\, \mathcal{U} \,\} \quad \text{into } D \times \{\, \mathbf{f}(\mathcal{U}) \,\} \\ \text{and therefore } \, \mathbf{f}/D \times \mathcal{U} = A_D \times P_A \, \mathbf{q}/\mathcal{U} \quad \text{and } P_A \, \mathbf{q}(\mathcal{U}) \subset C \, \mathcal{V} \,. \quad \text{Hence } \, \mathbf{V} \, \mathbf{q} = \mathbf{f} \,. \end{split}$$

Lemma 11. Let  $f: \widetilde{P} \longrightarrow \widetilde{R}$  be a continuous mapping such that  $f/B \times \{0\} \neq f_{B \times \{0\}}$ . Then f is constant.

Proof: Assume that  $f/B \times \{0\}$  is non-constant. Then Lemma 9 implies that  $f/B \times \{0\}$  is an embedding and so  $f(\langle x,0\rangle) = \langle x,1\rangle$  for every  $x \in B$ . Therefore  $f(\langle x,0\rangle) = \langle x,1\rangle$  for every  $f(B \times \{1\}) = \langle x,1\rangle$  and by Lemma 9 we have  $f(B \times \{1\}) = \langle x,1\rangle$ . Hence  $\langle x,1\rangle \in f(\Delta_X)$  and  $\langle x,1\rangle \in f(\Delta_X)$  which is a contradiction (see Lemma 9). Therefore  $f/B \times \{1\}$  is constant by Lemma 9. Analogously  $f/B \times \{1\}$  is constant and so is  $f/\Delta_X$ . Therefore  $f/A^X$  is constant by Lemma 9 and so is f.

<u>Definition</u>. Let  $\mathcal{K}$ ,  $\mathcal{L}$  be concrete categories. A functor  $\mathcal{D}: \mathcal{K} \longrightarrow \mathcal{L}$  is an almost full embedding of  $\mathcal{K}$  into  $\mathcal{L}$  if  $\mathcal{D}$  is an embedding of  $\mathcal{K}$  onto a subcategory of  $\mathcal{L}$  whose objects are  $\mathcal{D}(\alpha)$ ,  $\alpha$  running over objects of  $\mathcal{K}$  and whose morphisms are all non-constant  $\mathcal{L}$ -morphisms between these objects.

Theorem 12. Denote PAR the category of paracompact connected Hausdorff spaces and continuous mappings,
PAR a its subcategory with the same objects and continuous closed mappings as morphisms. Then each category L

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is almost universal in the sense that each concrete category has an almost full embedding into  ${\bf L}$  .

Theorem 12 follows from Construction 9 and Lemmas 10 and 11.

A class C of topological spaces is called <u>stiff</u> for every continuous mapping  $f: T \longrightarrow T'$ , with  $T, T' \in C$ , is either constant or the identity of the space T = T' onto itself.

V. Trnková had constructed a stiff class ( = not a set) of paracompact spaces as follows.

Let  $H_i$ , i=1,...,5 be five disjoint subcontinua of the Cook continuum. Choose points  $\alpha$ ,  $\nu$ ,  $\nu_2$ ,  $\nu_3 \in H_1$ ,  $\nu_i$ ,

$$Q_{\omega} = (\bigcup_{\alpha \in \omega} H_{1}^{\alpha} \setminus \{ \mathcal{L}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{2}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{2}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{2}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{2}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{2}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha} \setminus \{ \mathcal{L}_{1}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{3}^{\alpha} \} ) \cup (\bigcup_{\substack{i = 2/3 \\ \alpha \in \omega}} H_{i}^{\alpha}, \mathcal{L}_{3}^{\alpha}, \mathcal{L}_{4}^{\alpha}, \mathcal{L}_{4}^{\alpha},$$

 $G = Q_{\omega}$  is open iff it fulfils (1) - (5).

- (1)  $g_{i}^{\alpha}(G \cap H_{i}^{\alpha})$  is open in  $H_{i}$  for all i = 1, ..., 5,  $\alpha \leq \omega$ ;
- (2) if  $\alpha \in \omega$ ,  $\alpha \in G$  then

 $g_4^{\circ}(G \cap H_4^{\circ})$  is a mbh of  $x_4$  in  $H^4$  whenever  $\alpha = 0$ 

 $\varphi_{1}(G \cap H_{1}^{B})$  is a mbh of  $U_{1}$  in  $H_{1}$  whenever  $\alpha = \beta + 1$  G contains  $H_{1}^{T}$  for all  $\alpha' \leq \gamma < \alpha$  (and some  $\alpha' < \alpha$ ) whenever  $\alpha$  is limit;

- (3) if  $\alpha \in \omega$ , i = 2, 3,  $n_i^{\alpha} \in G$ , then  $g_i^{\alpha} (G \cap H_i^{\alpha})$  contains a *mbh* of  $n_i$  in  $H_i$ ;
- (4) if  $\kappa_5^{\omega} \in G$  then G contains  $H_1^{\gamma}$  for all  $\alpha' \leq \gamma < \omega$  (and some  $\alpha' < \omega$ ).
- (5) if  $s_5^{\omega} \in \mathcal{G}$ , then  $g_i^{\infty}(\mathcal{G} \cap \mathcal{H}_i^{\infty})$  contains a mbh of  $s_i$  in  $\mathcal{H}_i$  for all  $(i, \infty) = (0, 4), (\omega, 5)$  or i = 2, 3 and  $\infty \in \omega$ .

By means of Lemma 7, one can prove that  $\{Q_{\omega} \mid 1 \le \infty \}$  is a stiff proper class of paracompact spaces.

The existence of a stiff proper class of paracompact spaces follows also from the main result because "large discrete category" can be almost fully embedded in PAR.

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(Oblatum 17.9.1974)