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such that $f_2(x_1(h_1(t))) \geq \delta_4$ for $t \geq T_4 \geq \gamma(T_3)$. Further we proceed analogously as in the case I-1) we obtaining $x_2(t) < 0$ for large t , which contradicts $x_2(t) > 0$ for $t \geq t_1$.

2) Suppose that $x_1(t) > 0$, $x_2(t) < 0$ for $t \geq t_1$. (The proof in the case $x_1(t) < 0$, $x_2(t) > 0$ is similar). Then in view of (24), (25) from (A) we get $x_i^{(n)}(t) < 0$, $i = 1, 2$, for $t \geq t_2 = \gamma(t_1)$. Using Lemma, we have $x_1'(t) > 0$ and either i) $x_2'(t) < 0$, $x_2''(t) < 0$, or ii) $x_2'(t) > 0$ for $t \geq t_3 \geq t_2$. In the case i) we proceed in the same way as in the case I-2), obtaining a contradiction to the assumption $x_1(t) > 0$ for $t \geq t_1$. Now we consider the case ii). The component $x_2(t)$ is increasing and $\lim_{t \rightarrow \infty} x_2(t) = -b \leq 0$. If we suppose that $b > 0$, we proceed in the same way as in the case i) arriving at a contradiction. Therefore $b = 0$, i.e. $\lim_{t \rightarrow \infty} x_2(t) = 0$. This in view of Lemma implies $\lim_{t \rightarrow \infty} x_2^{(k)}(t) = 0$ for $k = 0, 1, \dots, n$.

The proof of Theorem 4 is complete. \square

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