

Werk

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and $t|\alpha_i| < i^{-2}$ for all $i = 1, 2, \dots$. Hence $F(tx) = 0$ and $(tx, 0) \in C_r(F, z_0)$. It means $L \subset C_r(F, z_0)$ and so (v) is verified.

On the other hand, (1.3) is violated. In fact, let

$$z_n = \frac{1}{n} (e_n, 0), \quad n = 2, 3, \dots$$

Then $z_n \rightarrow (0, 0)$ and for each $x = \sum_{i=1}^{\infty} \alpha_i e_i \in X$ we have

$$\|z_n - (x, Fx)\| = \max \left(\left\| \frac{1}{n} e_n - x \right\|, |Fx| \right) \geq \frac{1}{2} \left| \frac{1}{n} - \alpha_n \right| + \frac{1}{2} |Fx|.$$

If $\alpha_n < n^{-2}$, then

$$\|z_n - (x, Fx)\| \geq \frac{1}{2} \left| \frac{1}{n} - \alpha_n \right| > \frac{1}{2} \left(\frac{1}{n} - \frac{1}{n^2} \right) \geq \frac{1}{4} \cdot \frac{1}{n} = \frac{1}{4} \|z_n\|.$$

If $\alpha_n \geq n^{-2}$, then

$$\|z_n - (x, Fx)\| \geq \frac{1}{2} \left| \frac{1}{n} - \alpha_n \right| + \frac{1}{2} |\alpha_n| \geq \frac{1}{2} \cdot \frac{1}{n} = \frac{1}{2} \|z_n\|.$$

Hence

$$d(z_n, F) > \frac{1}{4} \|z_n\|, \quad n = 2, 3, \dots$$

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