

Werk

Label: Table of literature references

Jahr: 1978

PURL: https://resolver.sub.uni-goettingen.de/purl?31311157X_0103|log98

Kontakt/Contact

Digizeitschriften e.V.
SUB Göttingen
Platz der Göttinger Sieben 1
37073 Göttingen

✉ info@digizeitschriften.de

parallel to the coordinate axes. Choose $x^0 \in A(x, X \setminus K) \cap (X \setminus D)$. Applying Proposition 8, there is $y^0 \in A(x, X \setminus K)$ such that

$$y_{n+1}^0 < \min_{x \in D} x_{n+1}.$$

Again by Proposition 8, $B = A(y^0, X) \subset A(x, X \setminus K)$.

17. Proposition. *Let E be a compact subset of X . If E is convex (or more generally, if the set $\{x \in E; x_{n+1} = c\}$ is convex for each $c \in R$) then $r(E) = r(E^*) = E$.*

Proof. Consider $x^0 \in X \setminus E$ and let P be an arbitrary line which contains x^0 , $P \subset \{x \in X; x_{n+1} = x_{n+1}^0\}$. Consider $A(x^0, X \setminus E)$ and denote by P_1 the half-line starting from x^0 for which $P_1 \cap E = \emptyset$. Then according to Proposition 8, $P_1 \subset A(x^0, X \setminus E)$, i.e. $A(x^0, X \setminus E)$ is unbounded. This means $x^0 \notin r(E)$. Thus we have $r(E) \subset E$. Obviously $E \subset r(E)$. Analogously we can show that $r(E^*) \subset E$. Further, if $x^0 \in \text{int } E$, then $\text{int } E$ is closed and open — hence also finely open — in $X \setminus E^*$. By [2] $\text{int } E$ is an absorbent set in $X \setminus E^*$. Hence $A(x^0, X \setminus E^*) \subset \text{int } E$, i.e. $A(x^0, X \setminus E^*)$ is bounded and $x^0 \in r(E^*)$. Simultaneously $E^* \subset r(E^*)$ and this completes the proof.

References

- [1] *H. Bauer*: Harmonische Räume und ihre Potentialtheorie, Springer Verlag, Berlin, 1966.
- [2] *Ch. Berg*: Quelques propriétés de la topologie fine dans la théorie du potentiel et des processus standard, Bull. Sci. Math. 95 (1971), 27—31.
- [3] *C. Constantinescu* and *A. Cornea*: Potential theory on harmonic spaces, Springer Verlag, Berlin, 1972.
- [4] *R.-M. Hervé*: Recherches axiomatiques sur la théorie des fonctions surharmoniques et du potentiel, Ann. Inst. Fourier 12 (1962), 415—571.
- [5] *J. M. Landis*: Equations of the second order of elliptic and parabolic types (Russian), Nauka, Moscow, 1971.
- [6] *P. A. Loeb*: An axiomatic treatment of pairs of elliptic differential equations, Ann. Inst. Fourier 16, 2 (1966), 167—208.
- [7] *J. Lukeš* and *I. Netuka*: The Wiener type solution of the Dirichlet problem in potential theory, Math. Ann. 224 (1976), 173—178.
- [8] *N. Wiener*: Certain notions in potential theory, J. Math. Massachussetts 3 (1924), 24—51.

Author's address: 186 00 Praha 8, Sokolovská 83, ČSSR (Matematicko-fyzikální fakulta UK).