

## Werk

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**Definition 2.** Let  $L$  be a lattice and  $c \in L$ . If for each  $a, b \in L$  the element  $c$  fulfils the identity

$$(a \vee c) \wedge (b \vee c) = (a \wedge b) \vee c,$$

$c$  is called a *semi-distributive element*.

**Theorem 3.** Let  $L$  be a modular lattice and  $j \in L$  a semi-distributive element. Let  $J$  be a principal ideal generated by  $j$  and  $T_J$  the relation induced by  $J$ . Then  $T_J$  is a congruence relation on  $L$  (with the kernel  $J$ ).

**Proof.** By Theorem 2 in [3],  $T_J$  is a compatible relation for the principal ideal  $J$  generated  $j$  (it means  $J = \{x \in L; x \leq j\}$ ). By Theorem 1,  $T_J$  is a congruence relation on  $L$ . Clearly,  $J$  is the kernel of this congruence.

#### References

- [1] Hashimoto J.: Ideal Theory for Lattices, Math. Japonicae 2, (1952), 149—186.
- [2] Szász G.: Introduction to lattice theory, Akadem. Kiadó, Budapest 1963.
- [3] Chajda I.: A construction of tolerances on modular lattices, Časop. pěst. matem. 101 (1976) Praha, 195—198.
- [4] Chajda I., Zelinka B.: Compatible relations on algebras, Časop. pěst. mat. 100 (1975) Praha, 355—360.

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