

## Werk

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is obvious. Hence  $7^\circ \rightarrow 8^\circ$ . Also, the implication  $8^\circ \rightarrow 1^\circ$  is immediate. It remains to prove the implication  $2^\circ \rightarrow 7^\circ$ .

Suppose that  $2^\circ$  is satisfied and let us prove the following fact. If  $x_0 \in U$  and if  $V$  is a  $\sigma(E, A'E'_2)$  neighbourhood of  $x_0$  then there exists a  $\sigma(E, T'E'_3)$  neighbourhood  $W$  of  $x_0$  such that  $W \cap U \subset V$ . First of all, there exist  $f_1, \dots, f_n \in E'_2$  such that  $|\langle x - x_0, A'f_j \rangle| < 1$  for  $j = 1, 2, \dots, n$  implies  $x \in V$ . According to  $2^\circ$ , each  $A'f_j$  has a decomposition of the form

$$A'f_j = T'g_j + h_j$$

where  $g_j \in E'_3$  and  $h_j \in \frac{1}{4}U^0$ . Denote by  $W$  the set

$$W = \{x; |\langle x - x_0, T'g_j \rangle| < \frac{1}{2}\}.$$

If  $x \in W \cap U$ , we have, for each  $j$

$$|\langle x - x_0, A'f_j \rangle| \leq |\langle x - x_0, T'g_j \rangle| + |\langle x - x_0, h_j \rangle| < 1$$

so that  $x \in V$ . The proof is complete.

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