

Werk

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Proof. Denote $S_x = \{(t, t+x) \mid t \in M_x\}$ for a given x and

$$S = \bigcup_x S_x = \bigcup_x \{(t, t+x) \mid t \in M_x\}.$$

Since $(t, x) \in S$ if and only if $t \in M_{x-t}$ and M_r , $0 \leq r \leq 1$ are disjoint sets, it is evident that to a given t there is at most one x such that $(t, x) \in S$.

Denote by $P: R^2 \rightarrow R$ the projection $P(t, x) = x$. Since $P(S_x) = M_x + x$ and the sets $M_r + r$ are disjoint, we conclude again that to a given x there is at most one t such that $(t, x) \in S$.

Finally, $\{t \mid (t, t+x) \in S\} = \{t \mid t \in M_x\}$ for a given x , $0 \leq x \leq 1$. Hence $m^*\{t \mid (t, t+x) \in S\} = m^*(M_x) = 1$ and $m_*\{t \mid (t, t+x) \in S\} = m_*(M_x) = 0$.

Let $F(t, x)$ be defined by

$$\begin{aligned} F(t, x) &= \{0\} & \text{for } (t, x) \notin S, \\ F(t, x) &= [0, 1] & \text{for } (t, x) \in S. \end{aligned}$$

Then (4.6) to (4.8) imply (0.13) to (0.15).

References

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