

Werk

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where $K = \sum_{i=1}^n \sup_{t \in R^1} |g_i - \bar{g}_i|^*(t)$. The last inequality contradicts (2.5), which implies our assertion.

Proof of Theorem 2.2. Let (a_1, b_1) and (a_2, b_2) be two intervals such that $(a_1, b_1) \cap (a_2, b_2) \neq \emptyset$, $[a_1, b_1] \cup [a_2, b_2] \subset (a, b)$ and $\sum_{i,j=1}^n \int_{a_r}^{b_r} L_{ij}(t) dt < 1$ for $r = 1, 2$. Moreover, let $\beta > 0$ and $a_1 + \beta, b_1 - \beta \in (a_1, b_1)$, $a_2 + \beta, b_2 - \beta \in (a_2, b_2)$, $(a_1 + \beta, b_1 - \beta) \cap (a_2 + \beta, b_2 - \beta) \neq \emptyset$ and $t_0 \in (a_1 + \beta, b_1 - \beta)$. We consider the sequence $\{g_{iv}\}$ defined as follows

$$(3.10) \quad g_{i0}(t) = y_i^0, \quad g_{iv}(t) = y_i^0 + \int_{t_0}^t f_i(g_{1v-1}(s), \dots, g_{nv-1}(s)) ds, \\ i = 1, \dots, n, \quad v = 1, \dots, \quad t \in (a, b).$$

It is not difficult to verify that the sequence of functions $\{g_{iv}^*(t)\}$ is uniformly convergent to a function g_i ($i = 1, \dots, n$) of bounded variation in the interval $[a_1 + \beta, b_1 - \beta]$. Moreover, the system of functions $(g_1(t), \dots, g_n(t))$ is the unique solution of the problem (2.11) in the class $V_{(a_1 + \beta, b_1 - \beta)}^n$. Applying the property (P) we can extend uniquely the local solution to the whole interval (a, b) , which completes the proof of Theorem 2.2.

References

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