

Werk

Label: Table of literature references

Jahr: 1977

PURL: https://resolver.sub.uni-goettingen.de/purl?31311157X_0102|log11

Kontakt/Contact

[Digizeitschriften e.V.](#)
SUB Göttingen
Platz der Göttinger Sieben 1
37073 Göttingen

✉ info@digizeitschriften.de

have $x_{i+1} \in M_i$, $x_{i+1} \in M_{i+1}$, thus $M_i \cap M_{i+1} \neq \emptyset$, which means $(M_i, M_{i+1}) \in \mathcal{N}$, where \mathcal{N} is the tolerance on \mathfrak{M}_T defined above, for $i = 1, \dots, n - 1$. This means that $(M_1, M_n) \in \mathcal{C}(\mathcal{N})$ and the sets M_1, M_{n-1} are contained in the same class of the partition hull of \mathfrak{M}_T . As $a = x_1 \in M_1$, $b = x_n \in M_{n-1}$, the elements a, b are in the same class of the partition hull of \mathfrak{M}_T . As a and b were chosen arbitrarily, each equivalence class of $C(T)$ is contained in a class of the partition hull of \mathfrak{M}_T . Now let $c \in M$, $d \in M$ and let c and d be contained in the same class of the partition hull of \mathfrak{M}_T . Then there exist sets M'_1, \dots, M'_n of \mathfrak{M}_T such that $c \in M'_1$, $d \in M'_n$ and $M'_i \cap M'_{i+1} \neq \emptyset$ for $i = 1, \dots, n - 1$. For each i from the numbers $1, \dots, n - 1$ we choose an element $y_i \in M'_i \cap M'_{i+1}$. We have $c T y_1$, $y_n T d$ and $y_i T y_{i+1}$ for $i = 1, \dots, n - 1$. Thus $c C(T) d$. As c and d were chosen arbitrarily, each class of the partition hull of \mathfrak{M}_T is contained in an equivalence class of $C(T)$. The assertion is proved.

References

- [1] *G. Birkhoff*: Lattice Theory, Amer. Math. Soc. New York 1940.
- [2] *G. Birkhoff*: On the structure of abstract algebras. Proc. Cambridge Phil. Soc. 31 (1935), 433–454.
- [3] *G. Birkhoff* and *J. Frink*: Representation of lattices by sets. Trans. Amer. Math. Soc. 64 (1948), 299–316.
- [4] *N. Funayama* and *T. Nakayama*: On the distributivity of a lattice of lattice-congruences. Proc. Imp. Acad. Tokyo 18 (1942), 553–554.
- [5] *G. Grätzer*: Universal Algebra, Van Nostrand Co., London 1968.
- [6] *G. Grätzer*: Lattice Theory First Concepts and Distributive Lattices, Freeman and Co., San Francisco 1971.
- [7] *I. Chajda* and *B. Zelinka*: Tolerance relations on lattices. Čas. pěstov. mat. 99 (1974), 394–399.
- [8] *I. Chajda* and *B. Zelinka*: Compatible relations on algebras. Čas. pěstov. mat. 100 (1975), 355–360.
- [9] *I. Chajda* and *B. Zelinka*: Weakly associative lattices and tolerance relations. Czech. Math. J. 26 (1976), 259–269.
- [10] *I. Chajda*, *J. Niederle* and *B. Zelinka*: On existence conditions for compatible tolerances, Czech. Math. J. 26 (1976), 304–311.
- [11] *G. Szász*: Introduction to Lattice Theory. Akadémiai Kiadó Budapest 1963.
- [12] *E. C. Zeeman*: The topology of the brain and visual perception. In: The Topology of 3-Manifolds, ed. by M. K. Fort, pp. 240–256.
- [13] *B. Zelinka*: Tolerance graphs. Comment. Math. Univ. Carol. 9 (1968), 121–131.
- [14] *B. Zelinka*: Tolerance in algebraic structures. Czech. Math. J. 20 (1970), 179–183.
- [15] *B. Zelinka*: Tolerance in algebraic structures II. Czech. Math. J. 25 (1975), 175–178.

Authors' addresses: I. Chajda, 750 00 Přerov, Tř. Lidových milicí 290; B. Zelinka, 461 17 Liberec, Komenského 2 (Katedra matematiky a deskriptivní geometrie VŠST).