

## Werk

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and the existence of  $\varrho, \sigma$  such that

$$\begin{aligned}c_1 + c_3 &= \varrho(b_4 + b_6), & c_5 + c_7 &= -\varrho(b_1 + b_3), \\c_2 + c_4 &= \sigma(b_4 + b_6), & c_6 + c_8 &= -\sigma(b_1 + b_3).\end{aligned}$$

Thus  $L_3 = 0$  and our Theorem follows from (2.16). QED.

**Theorem 10.** Suppose: (i)  $M$  is compact, (ii)  $I_2 = \text{const.} \neq 0$  on  $M$ , (iii)  $K \geq 0$  on  $M$ , (iv)  $K^* > 0$  on  $f(M) \subset N$ . Then  $K = 0$  on  $M$  and  $\dim f_*(T_m(M)) \leq 1$  for each  $m \in M$ .

*Proof.* From  $I_2 = \text{const.}$  and (1.8),

$$\begin{aligned}(a_1 - a_4)(b_1 - b_5) + (a_2 + a_3)(b_2 + b_4) &= 0, \\(a_1 - a_4)(b_2 - b_6) + (a_2 + a_3)(b_3 + b_5) &= 0,\end{aligned}$$

and we may write

$$\begin{aligned}b_1 - b_5 &= \varrho(a_2 + a_3), & b_2 + b_4 &= -\varrho(a_1 - a_4), \\b_2 - b_6 &= \sigma(a_2 + a_3), & b_3 + b_5 &= -\sigma(a_1 - a_4)\end{aligned}$$

for suitable functions  $\varrho, \sigma$ . Thus  $L_1 = 0$ , and our Theorem follows from (2.2). QED.

The last theorem presents an interesting characterisation of the flat tori: In the class of compact surfaces with  $K \geq 0$  just the flat torus might be mapped into a positively curved  $N$  in such a way that  $I_2 = \text{const.} \neq 0$ . It is obvious that the conditions (iii) + (iv) of Theorem 10 may be replaced by (iii')  $K \leq 0$  on  $M$ , (iv')  $K^* < 0$  on  $f(M) \subset N$ .

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