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such that it has a fundamental branch B_0 isomorphic to B_1 and containing a vertex $v \in I_{\gamma(T)}(T_0)$ such that if we delete v from B_0 we obtain a branch isomorphic to B_2 .

We say that $B \in X$ is extraordinary if simultaneously (a) there is no $B' \in X$ such that $B' \rightarrow B$, (b) there is $B'' \in X$ such that $B \rightarrow B''$, and (c) $g(B, T_0) = g(B)$, for any $T_0 \in R$. If $B \in X$ fulfils (a), then it is isomorphic to a focus branch B_0 of T ; if moreover B fulfils (b), then B_0 has at least two edges and it contains a γ -vertex. It is easy to see that if B is extraordinary then all focus branches of T which contain any γ -vertex are isomorphic to B ; thus X contains at most one extraordinary branch.

By G we denote the directed graph with the vertex set X which is defined by the binary relation \rightarrow . Obviously, G is acyclic. Every vertex B of G is evaluated by the positive integer $g(B)$. Now, we define a new evaluation $h(B)$, for every $B \in X$, as follows: (i) if B is extraordinary, then $h(B) = g(B) + 1$; (b) if B is not extraordinary and if there is no $B' \in X$ such that both $B' \rightarrow B$ and $h(B') \neq 0$, then $h(B) = g(B)$; (c) if B is not extraordinary and if there is $B' \in X$ such that $B' \rightarrow B$ and $h(B') \neq 0$, then $h(B) = g(B) - 1$. As G is acyclic, $h(B)$ is uniquely determined for every $B \in X$.

Let $B \in X$. Then B is isomorphic to no focus branch of T if and only if $g(B) = 1$ and there is $B' \in X$ such that $B' \rightarrow B$ and B' is isomorphic to a branch of T . B is isomorphic to exactly $n \geq 1$ focus branches of T if and only if either (a) B is extraordinary, and $g(B) = n - 1$, or (b) B is not extraordinary, $g(B) = n$, and there is no $B' \in X$ such that $B' \rightarrow B$ and B' is isomorphic to focus branch of T , or (c) B is not extraordinary, $g(B) = n + 1$ and there is $B' \in X$ such that $B' \rightarrow B$ and B' is isomorphic to any focus branch of T . By induction we have the result that every $B \in X$ is isomorphic to exactly $h(B)$ focus branches of T . As every focus branch of T is isomorphic to some $B \in X$ and since we know the number of foci of T , then T can be reconstructed. The case when $|F(T)| = 1$ is obvious. If $|F(T)| = 2$, then T has exactly two focus branches; they have one common edge joining the foci.

References

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