

## Werk

**Label:** Figure

**Jahr:** 1986

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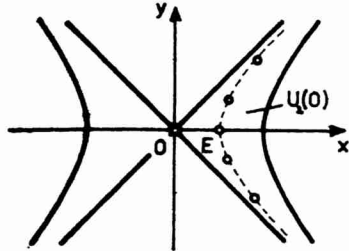


Fig. 1

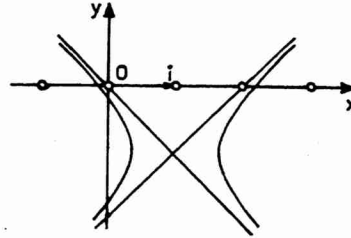


Fig. 2

then each  $U_r(X)$  or  $\tilde{U}_r(X)$  for which  $X$  is the point  $(1, -1)$  contains at least two members of the orbit  $O^B$ . Hence we ask how new conditions must be formulated? Are  $B(\mathcal{G})$  and  $B(\underline{1})$  certain 'discontinuous' motion groups if we suppose that one of the conditions which follow

$$\forall_{P, X} \exists_{r > 0} \text{card}(U_r(X) \cap P^B) \leq 2 \quad (2')$$

or

$$\forall_{P, X} \exists_{r > 0} \text{card}(\tilde{U}_r(X) \cap P^B) \leq 2 \quad (2'')$$

is true? Under which condition is (3) or

$$\forall_P \exists_{r > 0} \text{card}(\tilde{U}_r(P) \cap P^B) = 1 \quad (3)$$

fulfilled? We will give the answer in Section 2.

Now we will concentrate on two cases: normed plane and pseudo-Euclidean plane.

## 2. The discontinuous motion groups of the normed plane

It is well known that a distance function is given in every normed plane  $\mathbb{R}^2$ . So we can regard the unit circle  $k$  which is the gauge line (Eichfigur by H. MINKOWSKI [14] - see Fig. 3).

On the other hand, the norm  $\|\cdot\|$  of the normed plane  $\mathbb{R}^2$  is determined completely by  $k$ . Furthermore, every symmetric and convex curve which intersects each half-line by the point  $O$  just at one point has just one norm.

The isometries of  $\mathbb{R}^2$  called motions. For instance, the translations and the reflections in points are such transformations. Each motion of the plane  $\mathbb{R}^2$  is affine (see MAZUR and ULAM [13]) and a product of a motion for which  $O$  is a fixed point and of any translation. It is therefore sufficient to describe the subgroup  $G_0$  of such motions which have the fixed point  $O$ . These motions map  $k$  onto itself.

For each norm there is a unique Euclidean metric. In fact, there